

Date:

Name:

1. Calculate the unknown number in these proportions:

$J \Lambda \qquad 2.5 \qquad 0 \qquad J \ 2 \qquad \qquad \Lambda \ 2 \qquad 12 \ \Lambda \qquad J \ \Lambda \qquad \Lambda$	a. $\frac{2}{3} = \frac{5}{x}$	b. $\frac{5}{2.5} = \frac{x}{8}$	c. $\frac{x}{9} = \frac{12}{24}$	d. $\frac{2}{x} = \frac{5}{2}$	e. $\frac{4}{12} = \frac{12}{x}$	f. $\frac{18}{5} = \frac{7}{x}$	g. $\frac{4}{x} = \frac{x}{9}$
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## **Directly Proportional Problems**

We say that there is a **direct proportionality** between two magnitudes if an *increase* on one magnitude causes a proportional *increase* on the other and a *decrease* on the first quantity causes a proportional *decrease* on the second.

Note that a direct proportion is the same as proportions we have seen on the previous point. A direct proportion is also called simple proportion.

- 2. If two pencils cost \$1.50, how many pencils can you buy with \$9?
- 3. Jane ran 100 meters in 15 seconds. How long did she take to run 1 meter?
- 4. If  $\frac{4}{7}$  of a tank can be filled in 2 minutes, how many minutes will it take to fill the whole tank?
- 5. Richard earns \$17.5 for working 7 hours. How much will he earn for working 9 hours.
- 6. For cooking a cake for 6 people the recipe says that we need 3 eggs, 150g of flour and 50 g of sugar. Calculate how much of each ingredient we need to cook a cake for 9 people.
- 7. Mara has exchanged \$325 and has received 250€ without any commission. How much in € will she receive for \$19.50? How much in \$ will she receive for 60€?
- 8. My car uses 16 litres of petrol to travel 250 km. a) How far can I travel with 55 litres? b) How much petrol would I need to travel 180 km?

## **Inversely Proportional Problems**

We say that there is an **inverse proportionality** between two magnitudes if an *increase* in one magnitude causes a proportional *decrease* in the other and a *decrease* in the first magnitude causes a proportional *increase* in the other. That is if one magnitude is multiplied by 2, 3, ... this causes in the second a division by 2, 3, ... etc.

The most common example of inverse proportion problems would be "the more men on a job the less time taken for the job to complete"

- 9. If 18 men can do a job in 10 days, in how many days will 45 men do the same job?
- 10. It takes 12 hours for 3 bricklayers to build a wall. How long will it take for 5 bricklayers?
- 11. A company needs 33 workers to pack its production in 25 days, if the total production needs to be packed in 15 days. How many extra workers do they need?
- 12. It takes 4 men 6 hours to repair a road. How long will it take 12 men to do the job if they work at the same rate?
- 13. A truck that carries 3 tons need 15 trips to carry a certain amount of sand. How many trips are needed to carry the same amount of sand with another truck that carries 5 tons?
- 14. An automobile factory produces 8100 vehicles in 60 days. With the production rhythm unchanged. How many units will be made in one year?



## **Proportionality Problems**

- 15. Arthur is typing a paper that is 390 words long. He can type 30 words in a minute. How long will it take for him to type the paper?
- 16. Two pumps take 5 days to empty a pool. How long will 5 pumps take to empty the same pool?
- 17. It takes 175 minutes to drive home at 80 km/hr. How long will it take to drive home at 100 km/hr?
- 18. Two hydraulic shovels make the trench for a telephone cable in ten days. How long will it take to make the trench with 5 shovels?
- 19. Three tickets to a concert costs 60 euros. How much would five tickets cost?
- 20. A cyclist takes 6 minutes to cover 2 kilometres. How long would he take to cover 15 km?
- 21. A factory produces 1,400 pairs of trousers in one week (7 days). How many pairs of trousers does it produce in one month (30 days)?
- 22. A driver takes 3,5 hours to drive 329 km. How long will it take another trip in similar conditions as the previous one, but travelling 282 km instead?
- 23. A 300 gr wedge of cheese costs 6 euros. How much would a 450 gr wedge of cheese cost?

## Percentages

- 24. The population of a town is 652000 and 35% of them live in the centre district. How many of them live in this district?
- 25. 15% of the players in a football team have injuries. If the team has 20 players, how many players have injuries?
- 26. A cake weighs 1,200 gr. 10% of the cake's weight is butter. How many grams of butter are in the cake?
- 27. How much does a PS3 cost if its original price was 300 euros but a discount of 15% has been applied?
- 28. A hotel has 50 rooms and 35 of them are occupied. What percentage of the hotel's rooms are occupied?
- 29. 60 students at a school have signed up for a chess tournament. If they represent 15% of the total number of students, how many students does the school have?
- 30. In the class 13 students didn't do their homework; this was 52% of the class. How many students are in this class?
- 31. In a sale the price of a television set is 150€ which is 65% of the usual price, what was the original price?
- 32. The 6% of the population of Las Cabezas are immigrants and there are 960 immigrants living in our town, what is the population of Las Cabezas?
- 33. The price of some clothes is  $68 \in$  and there is a discount of 7%, what is the final price?
- 34. The population of a town is 63500 and last year it increased by 8%, what is the population now?
- 35. Last year there were 1560 employees in a company, this year 234 new people have been employed. What has been the % increase of the staff in the company?
- 36. The net salary of an employee is 1230€ after paying18% tax, what is the gross of his/her salary?
- 37. I have bought a pair of jeans for €24.20, the VAT is 21%, what was the price before VAT?

